Analysis of Heat Pipe Solar Collector with different Heat Pipe Parameter

B. Sivaraman*1 and N. Krishna Mohan*

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Abstract- Heat Pipe Solar Collector (hereafter referred as HPSC) has better collecting efficiency compared to the conventional collector, besides overcoming some of the drawbacks encountered with the later one. In this paper, numerical simulation & theoretical analyses of HPSC parameters are presented. The effects of $L_c/L_e$ (Condenser length /Evaporator length) ratio and $L/d_i$ (length/diameter) ratio of heat pipe on HPSC were analysed. Simulated results were compared with experimental values. Heat pipes (Five numbers each) having two different $L_c/L_e$, with two different $L/d_i$ have been designed, fabricated, and used in the solar collector absorber. Copper and Stainless steel have been used as container and wick material of heat pipe and Methanol has been used as working fluid. Heat pipes are designed to have heat transport factor of around 194 W and 260 W of thermal energy. The experiments were conducted during summer season with a collector tilt angle of 11° & 13° to the horizontal. It was found experimentally that the collector with less $L/d_i$ ratio was more efficient. This improved efficiency is due to increase in heat transport factor of heat pipe, which increases with decrease in $L/d_i$ ratio. Numerical simulation also shows that when the $L/d_i$ increases, the efficiency of the collector decreases. Similarly, the performance of HPSC was found to be better with higher $L_c/L_e$ value. The numerical simulation also has the same trend.

Keywords - Heat pipe, capillary limit, solar collector, wick, numerical simulation.

1. INTRODUCTION

The use of heat pipes in the field of solar energy has proved fruitful and solar water heater is one among the various applications of it. The thermal diode property, control over the temperature and efficient heat transfer capability of heat pipe can be effectively utilized by suitable design. Heat pipe in solar absorbers has many advantages over conventional collectors (instantaneous efficiency, 25-30%). It has superior heat conduction, thermal diode benefit and it responds quickly to any changes in radiation intensity. The major shortcomings of conventional solar collector are the liquid reverse motion during night and freezing of liquid in the tube during cold conditions. Such drawbacks can be overcome by replacing transport pipe with a heat pipe [1] - [19]. Bienert and Wolf [4] first reported the use of heat pipe in solar collectors. Soin et al [17], [18] investigated the performance of solar collector with fluid undergoing phase change and reported the effect of insolation and the liquid level on the collector performance of a thermosyphon collector containing acetone and petroleum ether. Akyurt [12] designed and tested the heat pipes on prototype solar water heater and found that heat pipes perform satisfactorily as heat transfer elements. Schreyer [14] reported that there was six percent increase in instantaneous efficiency, due to the use of refrigerant R-11 in a thermosyphon collector. Nesreen and Yvonne [13] fabricated and tested R-11 charged solar collector with an integrated condenser for secondary cooling water flow.


This paper presents the numerical simulation of HPSC. The parameters that were considered in the analysis are $L/d_i$, $L_c/L_e$, water inlet temperature, collector tilt angle and solar intensity, where $L$, $L_c$, $L_e$ and $d_i$ are total length, condenser length, evaporator length and inner diameter of heat pipe respectively.

2. DESCRIPTION OF THE SYSTEM

Design of Heat Pipes

Heat pipe is a very simple and efficient heat transfer device for transferring heat from a source to a sink by means of evaporation and condensation of a fluid in a sealed system. This sealed unit has a working fluid which absorbs the heat energy from the evaporator and transfers it to the condenser. The capillary action of wicks returns the condensate to the evaporator. The outstanding feature of heat pipe is its ability to accept heat non-uniformly (considerable change in the heat flux input may not affect the performance of the heat pipe). Heat pipes of 1 m total length with two different internal diameters and two different $L_c/L_e$ ratios were designed, fabricated, and used in the solar collector (Table 1) to study their effect on the performance of HPSC. Two sets of heat pipe (each set of five numbers) with copper pipe of 1 m total length; evaporator and condenser length of 0.85 m & 0.15 m
respectively having two different internal diameter of 17 mm and 19 mm were designed, fabricated and used in the HPSC to study the effect of L/d, ratio. To analyse the Lc/Le effect, another two sets of heat pipe (each set of five numbers) with internal diameter of 17 mm having two different evaporator and condenser length of 0.75, 0.85 m & 0.25, 0.15 m respectively were designed and fabricated. The maximum capillary limit (the heat load on heat pipe due to maximum capillary pressure for liquid wick combination) of the heat pipes were 194.25 W and 268.48 W. The designed heat transfer limit is sufficient to transfer the heat intercepted and gained by the absorber plate of the solar collector, as the maximum heat gained by the plate was around 300 W only. Such heat pipes (5 Numbers) were used in the solar collector and placed over the absorber plate (Fig.1). Wrapped screen wick structure with two layers of wick was used in the heat pipe (Fig.2).

![Fig. 1. Top view of the collector.](image)

![Fig. 2. Details of heat pipe.](image)

**Design of Solar Collector**

Solar collector is a flat plate collector (0.85 m x 0.5 m) with single glass covering. The collector absorber is a 2 mm thick black painted aluminum sheet. The heat pipes (5 Nos evenly spaced over the collector) were mounted on to the absorber sheet in such a way that the evaporator section of the heat pipe is within the collector and the condenser section is protruding outside the collector. The sides and back of the collector were properly insulated. All the five condenser sections of the heat pipes have been connected serially. The collector was placed facing directly south with different tilt angles to the horizontal, to study its effect on HPSC. Copper – Constantan thermocouples were provided in the collector to measure the temperatures of absorber plate, glass plate and surface of the heat pipe at two different locations on each heat pipe in the evaporator section, one being nearer to the condenser section.

![Table 1. Specifications of Heat pipes](image)

<table>
<thead>
<tr>
<th>Description</th>
<th>Pipe – 1</th>
<th>Pipe – 2</th>
<th>Pipe – 3</th>
<th>Pipe – 4</th>
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</thead>
<tbody>
<tr>
<td>Outer diameter of the heat pipe, m</td>
<td>0.019</td>
<td>0.022</td>
<td>0.019</td>
<td>0.019</td>
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<tr>
<td>Inner diameter of the heat pipe, m</td>
<td>0.017</td>
<td>0.019</td>
<td>0.017</td>
<td>0.017</td>
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<tr>
<td>Total length, m</td>
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<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
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<tr>
<td>Evaporator length, m</td>
<td>0.85</td>
<td>0.85</td>
<td>0.85</td>
<td>0.75</td>
</tr>
<tr>
<td>Condenser length, m</td>
<td>0.15</td>
<td>0.15</td>
<td>0.15</td>
<td>0.25</td>
</tr>
<tr>
<td>Wick mesh size number</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
</tr>
<tr>
<td>Capillary limit, W</td>
<td>194.25</td>
<td>268.48</td>
<td>194.25</td>
<td>194.25</td>
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<tr>
<td>Sonic limit, W</td>
<td>52578.78</td>
<td>62392.93</td>
<td>52578.78</td>
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<tr>
<td>Entrainment limit, W</td>
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<td>2800.4</td>
<td>2070.21</td>
<td>2070.21</td>
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<tr>
<td>Boiling limit, W</td>
<td>1784.81</td>
<td>1158.8</td>
<td>1784.81</td>
<td>1574.832</td>
</tr>
</tbody>
</table>

**Experimental Setup**

Experiments were conducted with the designed HPSC for two different mass flow rates (0.0033 & 0.0083 kg/s) on various days and observations were recorded every 20 min (10.00 A.M - 4.00 P.M). Solar intensity at the test site (Location: Annamalainagar, Latitude: 11° N) was measured using EPPLY pyranometer. The water inlet and exit temperatures were measured using mercury in glass thermometer. The flow rate was measured using graduated rotameter.

**3. NUMERICAL SIMULATION OF HEAT PIPE SOLAR COLLECTOR**

This section presents the detailed theoretical analysis of the heat pipe solar collector. The performance of the collector was studied by the numerical simulation procedure. The simulation procedure involves casting governing mathematical equations for each system components by balancing the energy into and out of it and then combining these models consecutively to accomplish complete simulation of the system. The heat pipe solar collector system components are glass cover, absorber plate, evaporator, wick, working fluid, condenser, circulating water and heat exchanger. The individual components governing equations were then non-dimensionalized and the resultant equation was written as finite difference equation form using Crank-Nicolson
method. The system of simultaneous equation was then solved.

**System component modelling**

A schematic sketch of the heat pipe solar collector under study is shown in Fig. 3. For the thermal analysis of the collector, the following assumptions were made to simplify the problem.

1. The entire system is in thermal equilibrium with the ambient.
2. Glass cover temperature is assumed uniform at any given instant.
3. The temperature gradient across the absorber plate thickness and across the thickness of the heat pipe wall may be neglected.
4. The temperature gradient in the longitudinal direction in the evaporator section can be neglected, since the evaporator section of heat pipe is subjected to constant solar energy.
5. The sides of the collector are well insulated, hence the edge losses are neglected in the analysis.
6. The bond resistance between the absorber and heat pipe are neglected.
7. Vapour temperature inside the heat pipe is that of saturation temperature.

The graph is titled **Fig. 3. Schematic of HPSC.**

The glass cover governing equation can be written in the dimensional form (W/m²)

\[ \rho_a C_v \frac{dT_g}{dt} = \frac{U_m}{h_{iga}} \left(T_g - T_a\right) - h_{iga} \left(T_g - T_a\right) \]

where

- \( U_m \) is the overall heat loss coefficient between the absorber plate and glass cover.
- \( h_{iga} \) & \( h_{iga} \) are the convective and radiation heat transfer coefficient between glass cover and ambient.

The absorber plate governing equation per unit area is given by (W/m²)

\[ \rho_a C_v \frac{dT_p}{dt} = k_a \frac{dT_p}{dx} + \left(T, h_{iga}\right) \frac{dT_p}{dx} - h_{iga} \left(T_a - T_g\right) \]

Subject to the boundary conditions given

\[ \frac{dT_p}{dx} = 0 \quad \text{at} \quad x = 0 \& w, \quad t \geq 0 \]

\[ T_p = T_c \quad \text{at} \quad x = x_c \quad t \geq 0 \]

where

\[ I_s, \] the global solar radiation is theoretically estimated using Lingamganta & Veziroglu [6] correlation

\[ U_s \] is the bottom loss coefficient of the collector.

The energy balance equation of the evaporator section is given by (W/m)

\[ \rho_v A_{ev} C_v \frac{dT_e}{dt} = \left(T, \alpha_e\right) \frac{dT_e}{dx} - k_e \frac{dT_e}{dx} \left( T_e - T_w \right) \]

\[ \frac{md}{2} U_e \left(T_e - T_w\right) - \pi d h_e \left(T_e - T_s\right) - k_{eff} L_e \left(T_e - T_w\right) \]

where \( k_{eff} \) is the effective thermal conductivity of the wick structure.

The heat transfer coefficient of evaporator is given by

\[ h_e = \frac{4}{3} \left[ \frac{\rho_i k' g h_{uw}}{4 \mu (T_e - T_s) L_e} \right] \]

The working fluid inside the heat pipe is fully saturated and its energy balance equation is given by (W)

\[ \frac{\pi d^2}{4} \rho_v V L C_v \frac{dT}{dt} = \pi d L h_e \left(T_e - T_s\right) - \pi d L h_c \left(T_e - T_s\right) \]

The energy balance of the heat pipe wick is given by (W/m³)

\[ \left( \rho C \right)_{w} \frac{dT}{dt} = k_{eff} \frac{\partial^2 T}{\partial y^2} \]

subject to the boundary conditions

\[ T_e = T_s \quad \text{at} \quad y = 0, \quad t \geq 0 \]

\[ \frac{dT}{dy} = 0 \quad \text{at} \quad y = L_e, \quad t \geq 0 \]

The heat transfer coefficient of condenser is given by

\[ h_c = \frac{4}{3} \left[ \frac{\rho_i k' g h_{uw}}{4 \mu (T_e - T_s) L_e} \right] \]

\( h_{fi} \) is the convective heat transfer coefficient of water flowing inside the heat exchanger.
The energy balance of the differential element of water inside the heat exchanger is given by (W/m)

\[ \rho_w C_w \frac{\partial T_w}{\partial t} + \dot{m}_w C_w \frac{\partial T_w}{\partial y} = \pi d h_o (T_w - T_e) - \pi d h_w (T_e - T_w) \]  

(13)

with the boundary condition

\[ T_w = T_{\text{sat}} \quad \text{at} \quad y = 0, \ t \geq 0 \]  

(14)

\( h_o \) is the outer convective heat transfer coefficient of the heat exchanger.

The energy balance of the differential element of a heat exchanger is given by (W/m)

\[ \rho_{\text{ex}} A_{\text{ex}} C_{\text{ex}} \frac{\partial T_{\text{ex}}}{\partial t} = k_{\text{ex}} A_{\text{ex}} \frac{\partial^2 T_{\text{ex}}}{\partial y^2} + \pi d h_{f_o} (T_w - T_{\text{ex}}) \]

\[ - \pi d U_{\text{ex}} (T_{\text{ex}} - T_a) \]  

(15)

with the following boundary conditions

\[ \frac{dT_{\text{ex}}}{dy} = 0 \quad \text{at} \quad y = 0 \ & \ L_c \ t \geq 0 \]  

(16)

The above governing equation of components and boundary conditions are converted into non-dimensional form to generalize the analysis by defining dimensionless parameters for coordinates, temperature, radiation and time as

\[ X = \frac{x}{w}, \ Y = \frac{y}{L_c}, \ \theta = \frac{k_p (T - T_a)}{I_{in} P}, \ \tau = \frac{k_p t}{\rho C_p P^2} \]  

(17)

\[ I_c = \frac{I_c}{I_{in}} \]

where \( I_{in} \) is the solar constant.

The non-dimensionalised governing equations are then written in finite difference form using Crank-Nicolson scheme for the partial differential equations and by modified Euler’s scheme for the ordinary differential equations. The absorber plate, condenser section of heat pipe, the circulating water and heat exchanger are discretized and solved.

**The simulation procedure**

The numerical procedure for solving the above set of finite difference equations is as follows:

The initial temperatures of all the components of the collector were set.

Non-dimensional time step of 0.001 was set for the simulation of collector performance.

The starting time and ending time of simulation were set.

Given the collector tilt angle, day of the year, collector configuration, cooling water inlet temperature, ambient temperature the simulation of the collector performance commences.

The output of the simulation was saved after each iteration and the output data were used for the theoretical analysis of the collector performance.

4. **RESULTS AND DISCUSSION**

**Experimental results**

Water was used as cooling fluid in the condenser of heat pipe. Figure 4 shows the instantaneous efficiency curve of the HPSC system for a day. A maximum collector efficiency of around 67\% was obtained during peak sunshine hour and the fluid outlet temperature of 318 K, while the fluid inlet temperature was kept at 308 K. Figure 5 shows the plot of efficiency curve for different L/d, ratio of heat pipe. It is very clear from the plot when the L/d, is reduced the performance of the collector improves.
In Fig. 5, the efficiency curve for the day 25.03.04 shows the lesser performance, since the condenser end of the heat pipe was kept at bottom, in which case the working fluid had to be transported only by capillary action of the wick. Figure 6 confirms that the working fluid flow is hampered by the position of the condenser. When the condenser section is kept at below the evaporator the temperature build up on the evaporator side is more due to slow transport of fluid to that section and hence the evaporation rate is less, ultimately resulted in poor performance of the collector system as it is shown in Figs. 7 & 8. From Fig. 8 it is also evident that the rise in temperature of water goes down as flow rate increases. Figure 9 show the plot of time vs. water outlet temperature of the collector for different flow rates of cooling water on the collector side. The curve is in good agreement that when flow rate increases the rise in water temperature decreases. Figure 10 shows the variation of water outlet temperature with different Lc/Le ratio. When that ratio was increased, the performance was good since the condensation rate got improved resulting in more quantity of working fluid flow to the evaporator at any given instant consequently increases the evaporation rate.

**Numerical results**

The set of governing equations of the system components of HPSC were simultaneously solved using the procedure given earlier and the temperature of individual components were obtained. Figure 11 compares the experimental and numerical prediction of water outlet temperature of the collector. The predicted results were in good agreement with the experimental values. The percentage error of the predicted value is less than ±5 percent at any given time. The error may be due to round off and truncation error of numerical method adopted and also due to instrumentation error of experimental data. The numerical results are within the allowable error limit.

![Fig. 6. Time vs. Evaporator temperature for different condenser position.](image)

**Fig. 5. Efficiency vs. Time for different L/di ratio.**
Fig. 7. Time vs. Efficiency with different L/d₁ ratio.

Fig. 8. Time vs. Water outlet temperature for different flow rate & L/d₁ ratio.

Fig. 9. Water outlet temperature vs. Time for different flow rate.
Fig. 10. Water outlet temperature vs. Time for different $L_c/L_e$ ratio.

Fig. 11. Experimental & Numerical result of $T_{outw}$.

Fig. 12. Effect of $L/d$ ratio on collector performance.
Figures 12 & 13 shows the effect of L/di ratio on the output water temperature and on one of the evaporator wall temperature of the HPSC for the similar conditions of other parameters. With decrease in L/di ratio, the water outlet temperature increases, where as the evaporator wall temperature decreases as expected which is due to accumulation of heat on the evaporator side due to less condensation rate on the condenser side of the heat pipe. Figure 14 shows the same effect of this ratio on the performance of collector when the Lc/La ratio was changed. Figure 15 shows that same trend is obtained when the absorber plate thickness was changed. The effect of Lc/Le ratio of heat pipe on the outlet temperature of HPSC is plotted in Fig. 16, which show that the predicted results are following the trend as expected. Though that variation is nil during the initial hours of exposure to sunlight, there exists a gradient as time passes and again the gradient decreases when the solar flux falls down. The variation of temperature is minimal, but 5 to 8 % increase in the instantaneous efficiency of the collector will be obtained for the same.

Figures. 17 & 18 show the effect of thickness of absorber plate (δp) on the water outlet temperature of the HPSC. The heat gained by the absorber with 2 mm thick is more during initial hours of exposure, but the response of 3 mm thick absorber overtake at later stage. The mass flow rate effect on the performance of the HPSC is plotted in Fig. 19. The trend of the curve shows the same trend as reported for the experimental work. The effect of heat pipe working fluid on the HPSC is reported in Figs. 20 & 21. The simulation was carried out for three working fluids namely for methanol, Acetone and water. Almost same performance was predicted for acetone and methanol. The heat exchanger dimensional parameter’s effect was shown in Fig. 22. The increase in the internal diameter of heat exchanger results in decrease in the outlet temperature of water. This may be due to increase in overall heat transfer coefficient of heat exchanger as a result of which more heat is transferred to the ambient.
Fig. 15. Effect of $L/d_i$ ratio on $T_{\text{wax}}$.

Fig. 16. Effect of $L_c/L_e$ ratio on $T_{\text{wax}}$.

Fig. 17. Effect of $\delta_p$ on $T_{\text{wax}}$. 
Fig. 18. Effect of $\delta_p$ on $T_{\text{water}}$.

Fig. 19. Effect of $m_w$ on $T_{\text{water}}$.

Fig. 20. Effect of working fluid on $T_{\text{water}}$. 
5. CONCLUSION

Numerical investigation on heat pipe solar collector had been carried out and the following conclusion is reported. The numerical prediction is well within the error limit on comparison with the experimental values. The effects of several parameters have been analysed in this numerical investigation and it was found that the L/d ratio and Lc/Le ratio have significant effect on the performance of the collector. Between the two low boiling working fluid, methanol has found to be more effective than other fluid. It was also found that the heat exchanger dimension and thickness of the absorber also have some effect on the performance of the collector.

**NOMENCLATURE**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td>$C$</td>
<td>specific heat, J/kg K</td>
</tr>
<tr>
<td>$d$</td>
<td>diameter, m</td>
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<tr>
<td>$h$</td>
<td>heat transfer coefficient, W/m$^2$ K</td>
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<td>$I$</td>
<td>Solar Intensity, W/m$^2$</td>
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<td>$\phi$</td>
<td>porosity of wick dimensionless</td>
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<td>$\mu$</td>
<td>dynamic viscosity, N s/m$^2$</td>
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</table>
\( \rho \) density, kg/m\(^3\)

\( \tau \) transmittance, dimensionless

**Subscripts**

\( a \) ambient

\( \alpha \) sky

\( b \) bottom

\( c \) condenser section

\( ccs \) wall cross-section of condenser section

\( cga \) convection between glass cover and ambient

\( e \) evaporator section

\( ecs \) wall cross-section of evaporator section

\( eff \) effective

\( eg \) evaporator to glass cover

\( ex \) heat exchanger

\( excs \) heat exchanger cross section

\( fi \) inner film heat transfer between condenser section and cooling water

\( fo \) outer film heat transfer between water and heat exchanger

\( g \) glass cover

\( i \) inside

\( l \) working fluid inside the heat pipe

\( o \) outer

\( p \) absorber plate

\( pg \) plate to glass cover

\( rga \) radiation between glass cover and sky

\( rgg \) radiation between absorber plate and glass cover

\( s \) saturation

\( t \) time, total

\( v \) vapour, vapour core

\( w \) water, wind

\( w_i \) inlet cooling water

\( w_{out} \) outlet cooling water

1 inside diameter of heat exchanger

2 outside diameter of heat exchanger

**REFERENCES**


